

# The Ideal Loan and the Patterns of Cross-Border Bank Lending

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12. Februar 2014

# Motivation

Gravity equations explain many cross-border activities very well, while often it is unclear why

We need a theoretical foundation, in order to...

- find the proper specification
- interpret the results correctly

# Theoretical gravity equations for bank loans

So far proposed theories to explain cross-border financial assets holdings focused on equity

- Portfolio investment (Martin und Rey 2004, JIE)
- Equity (Okawa und van Wincoop 2012, JIE)

Gravity equation results in general equilibrium

We offer a theoretical foundation for bank loans in a partial equilibrium that does *not* require portfolio optimization over all assets world wide

# Bank loans as differentiated customer-bank relationship

## The starting point:

- Bank loans are differentiated products, negotiated in a bank-firm-relationship
- A credit contract is *not* a homogeneous debt holding, where only the interest rate is relevant

## OECD interest rate definition (MEI)

"...interest rates vary not only because of inflation ... but also because of a number of other influences, including the amount, purpose and period of the transaction, the credit-worthiness of the borrower, the collateral offered and/or guarantees/guarantors available, the competition for the transaction, government policy. As a consequence, there will be numerous rates applying to a large number number of transactions that are in effect at any one time in any one country."

# Our steps

1. Specification of a possible firm-bank-relationship
2. Decision on the best offer by the firm
3. Aggregation over all firms
4. Derivation of the gravity equation for bank loans
5. Estimation with BIS data

# Outline

- 1 Story
- 2 Theory
- 3 Estimation
- 4 Concluding remarks

# The firm-bank-relationship

- A firm manager approaches a bank with the rough characteristics of a loan request
  - Amount needed, time schedule, and maturity
  - Fixed costs, interest rate and its adjustment
  - Collateral
  - Information requirements
- The bank makes a loan offer
- The manager approaches several banks to compare the offers

We assume, that...

- banks make take-it or leave-it offers
- the non-monetary characteristics of the offer can be quantified
- we therefore can compare credit costs  $c$

# Credit costs

Credit costs are specific for each relationship of firm  $g$  and bank  $k$ .

They depend on firm-specific, bank-specific and relationship-specific characteristics

Credit costs  $c_{gk}$

$$c_{gk} = \beta r_{gk} + \underbrace{\gamma \tau_{gk}}_{\text{relationship-specific}} + \underbrace{\delta a_k}_{\text{bank-specific}}, \quad (1)$$

where  $r_{gk}$  denotes the interest rate

## Average credit costs

Credit costs in (1) are data demanding → impossible to acquire for a large sample of different countries

We are interested on country characteristics anyway

We express the credit costs in (1) in country characteristics

Credit costs  $c_{gk}$

$$c_{gk} = \beta r_j + \underbrace{\gamma \tau_{ij}}_{\substack{\uparrow \\ \text{bilateral} \\ \text{variables}}} + \underbrace{\delta a_j}_{\substack{\downarrow \\ \text{credit} \\ \text{country-specific}}} + \epsilon_{gk}, \quad (2)$$

Index  $i$  denotes the country of the firm,  $j$  the country of the bank.  
 $\epsilon_{gk}$  might be known to the firm but not to the researcher

## Credit choice

The firm minimizes its credit costs by choosing among the offers the most suitable.

The probability, that firm  $g$  from  $i$  chooses the offer by bank  $k$  from  $j$  equals

$$\begin{aligned}
 \mathbf{P}_{igjk} &= \Pr(c_{igjk} = \min\{c_{l1} \cdots c_{ln_l}\}; \quad l = 1 \cdots N, jk \neq lh) \\
 &= \Pr(\bar{c}_{ij} - \bar{c}_{il} + \epsilon_{igjk} < \epsilon_{igl1}; \cdots; \bar{c}_{ij} - \bar{c}_{il} + \epsilon_{igjk} < \epsilon_{igln_l}) \\
 &= 1 - \Pr(\bar{c}_{ij} - \bar{c}_{il} + \epsilon_{igjk} \geq \epsilon_{igl1}; \cdots; \bar{c}_{ij} - \bar{c}_{il} + \epsilon_{igjk} \geq \epsilon_{igln_l}) \\
 &= \underbrace{\prod_{l=1}^N \prod_{\substack{h=1 \\ lh \neq jk}}^{n_l}} [1 - F(\bar{c}_{ij} - \bar{c}_{il} + x)], \quad l = 1 \cdots N
 \end{aligned}$$

We assumed that the non-observable components  $\epsilon$  are iid.

## Probability to choose bank $k$ from $j$

The probability that firm  $g$  chooses bank  $k$  from  $j$  can be approximated by an extreme value distribution if the number of banks is large  $n_j \rightarrow \infty$ .

In our case of normally distributed residuals  $\epsilon$ , the minima are Gumbel distributed with

$$1 - G(x) = \exp \left[ - \exp \left( \frac{x - \mu}{\sigma} \right) \right] \quad (3)$$

where the location parameter  $\mu$  and the scale parameter  $\sigma$  of the Gumbel distribution depend on variance of the residual  $\sigma_\epsilon$  and the number of banks  $n_j$ :  $\mu = \sigma_\epsilon \ln n_j$ ,  $\sigma = \sigma_\epsilon$

$x$  is any realization of the residual  $\epsilon$

## The probability to choose bank $k$ from $j$

...can also be expressed as

$$\mathbf{P}_{gijk} = \int_{-\infty}^{\infty} \frac{1}{\sigma} \exp\left(\frac{x - \mu}{\sigma}\right) \left\{ \exp\left[-\exp\left(\frac{x - \mu}{\sigma}\right)\right] \prod_{l=1}^N \exp\left[-\exp\left(\frac{\bar{c}_{ij} - \bar{c}_{il} + x - \sigma \ln n_l}{\sigma}\right)\right] \right\} dx. \quad (4)$$

Solving the integral yields for the probability

$$\mathbf{P}_{gijk} = \frac{n_j \exp\left(-\frac{\bar{c}_{ij}}{\sigma}\right)}{\sum_{l=1}^N n_l \exp\left(-\frac{\bar{c}_{il}}{\sigma}\right)}. \quad (5)$$

## A gravity equation for bank loans

Multiplying the probabilities with all bank loans demanded by firms in country  $i$  yields

$$BA_{ji} = \frac{n_j \exp\left(-\frac{\beta r_j + \gamma \tau_{ij} + \delta a_i}{\sigma}\right)}{\sum_{l=1}^N n_l \exp\left(-\frac{\beta r_l + \gamma \tau_{il} + \delta a_i}{\sigma}\right)} BL_i \quad (6)$$

a gravity equation explaining cross-border bank loans from  $j$  to  $i$

- The sum is a credit country-specific constant  $\rightarrow$  fixed effect
- The equation can be estimated as log-linearized version OLS or Poisson

# The BIS data

- Available upon request by the BIS
- Bilateral claims at the country-level disaggregated by various characteristics
- 2 approaches of aggregation: consolidated data (consolidated within the group), locational data (balance of payments principal)
  - We have chosen the locational data
- Split with respect to the type of borrower (bank vs non-bank)
  - We use only non-bank partners
- More than 80% of the claims have maturity → credits or bonds, not equity

# Regression model

We estimate (6) as:

$$BA_{ji} = \exp [(\beta_1 r_j + \beta_2 \tau_{ij} + D_j - D_i)] n_j^{\beta_3} BL_i^{\beta_4} \varepsilon_{ij}. \quad (7)$$

in a two-stage approach with

1.  $BA_{ji} = \exp [(\beta_1 \tau_{ij} + D_j - D_i)] \varepsilon_{ij}$

2.  $\tilde{D}_j = \gamma_1 r_j + \gamma_2 \ln n_j + \gamma_3 a_j + \xi_j$

- We estimated the first stage Poisson
- The second stage GLS using the variance of the estimated fixed effects as weights

# Explanatory variables

- $r_j$  Prime rate of banks from WDI and ECB Statistical Data Warehouse
- $\tau_{ij}$  different distance-dependent variables from CEPII
- $a_j$  Measure for the quality of the bank market mainly from Financial Structure Database (Beck and Demirguc-Kunt)
- $n_j$  effective number of banks approximated by the size of total assets of banks in country  $j$

All variables are aggregated or averaged at country-level

Time period: 2003 to 2006

17 credit countries, 144 loan receiving countries

# Results

## Panel Gravity equation for cross-border bank loans

	PPML	OLS	OLS ( $1+BA_{ij}$ )
distance	-0.26** [0.086]	-0.73** [0.065]	-0.83** [0.059]
contiguity	-0.02 [0.171]	-0.17 [0.174]	-0.33 [0.179]
common language	0.40 [0.205]	0.81** [0.103]	0.89** [0.100]
common legal origin	0.22* [0.087]	0.13 [0.076]	-0.03 [0.073]
Regional Trade Agreement	0.39** [0.136]	0.69** [0.132]	0.66** [0.120]
Common Currency	0.94** [0.124]	1.46** [0.125]	1.85** [0.129]
<i>N</i>	6331	4947	6331
<i>R</i> <sup>2</sup>	0.857	0.64	0.66

## Second stage

### Second stage: pooled cross-section regression

	(1)	(2)	(3)	(4)	(5)	(6)	(7)
Banking Market Size <sub><i>j</i></sub>	1.14** [0.116]	1.18** [0.153]	1.13** [0.134]	1.16** [0.111]	1.07** [0.112]	1.08** [0.109]	1.13** [0.113]
Interest Rate <sub><i>j</i></sub>	-0.10** [0.010]	-0.09** [0.012]	-0.10** [0.010]	-0.09** [0.010]	-0.10** [0.008]	-0.07** [0.008]	-0.07** [0.009]
3 Bank Concentration Ratio		0.75 [0.775]					
Return on Assets			-2.84 [20.494]				
Cost Income Ratio				-1.44 [1.072]			
Z-Score					-0.04 [0.026]		
Bank Asset to GDP <sub><i>j</i></sub>						1.08** [0.220]	
Bank Credit to GDP <sub><i>j</i></sub>							1.13** [0.233]
<i>N</i>	50	50	50	50	48	50	50
<i>R</i> <sup>2</sup>	0.859	0.863	0.859	0.864	0.857	0.892	0.897

## Discussion: Partial- versus general equilibrium models

- Partial equilibrium based analysis is a realistic modeling of cost comparison by firms
- It does neither require assumption of complete markets nor an optimization over all possible options with feed backs on all other loan contracts
- It accounts for relationship-specific loan contracts
- We work nevertheless with a possibly endogenous (affected by cross-border bank loans) interest rate

# Summary

- We derived a gravity equation for bank loans from the cost minimization of firms
- Starting point: A loans contract is seen as a differentiated product
  - Credit costs depend *not* only on the interest rate
- Firms search for the best offer
- Aggregation over all firms in country  $i$  and all banks  $j$  yields a gravity equation
- Estimation using BIS Data